Exploring Different Stages of Alzheimer’s Disease through Topological Analysis of Differentially Expressed Genetic Networks

Aurpan Majumder and Mrityunjay Sarkar

Abstract—Inter-organ dependency of different regions/genes in an eukaryote is nowadays a most challenging issue for researchers. Some neurodegenerative disorders (such as Alzheimer’s Disease (A.D)) in a particular organ (Brain) show differential expression patterns across different regions and they are affected by one another. In this work, we have proposed an extended version of an existing concept (Topological Overlap (T.O)). Here we have gone through a “weighted T.O” analysis approach which shows interdependency of all genes present in a network unlike “un-weighted T.O” which shows gene dependency of only some significantly connected genes in a network. The weighted as well as un-weighted counterpart helps us to understand the dependency of genes which are responsible for generation and spreading of A.D. Finally, we have ranked the genes (Differentially expressed across different stages of AD) upon the T.O value based permutation test/’t’-test’ and crosschecked the ranked results with a recently published novel ranking scheme. We have also checked the significance of top 15 genes from both methods. In result section we have shown that our method is better than existing one.

Index Terms—Alzheimer’s disease, G. O., KEGG pathways, topological overlap, weighted and un-weighted measure.

I. INTRODUCTION

Alzheimer’s disease (AD) is the most common form of dementia. It is an irreversible, progressive brain disease which is characterized by the development of amyloid plaques and neurofibrillary tangles, leading to the loss of connections between nerve cells, or neurons, in the brain, and the death of these nerve cells. With aging this problem becomes worse. In our work we check how genes affect human brain functionality upon aging that cause spreading of AD from one stage to another.

The rest of the paper is as follow. In next section we have given a brief Theory and literature review. Next we have discussed about the Methodology Then Results and Discussion with respect to other existing method is discussed. This paper concludes with Conclusion and Future work.

II. THEORY

A.D is of two types: early-onset and late-onset. Early-onset Alzheimer's disease occurs in people aged between 30 and 60 years. It is rare, representing less than 5 percent of all people who suffer from this disease. But most cases of Alzheimer's are the late-onset form, which develops after 65 years of age [1], [2]. Many factors are responsible for Alzheimer. Some researchers have suggested that it can be due to calcium-dependent K+ channels in platelets [3] while Lanne has given the concept the ryanodine receptors (RyRs) which is the major intracellular Ca²⁺ release channel [4] as a probable cause. However diets (proteins) [5], [6] and hormones may also play a pivotal role [7]-[10].

Together all these reasons cause neurodegenerative disease such as Alzheimer. In our work we have found genes responsible for the process that modulates the membrane potential involved in the propagation of a signal in a neuron (Results and discussion).This work also focuses on genes responsible for moving extracellular fluids to and from tissue within a multicellular organism which validates the reason of expansion of the Cerebral Spinal Fluid(CSF) space reducing the CSF turnover rate, thus compromising the CSF sink action to clear harmful metabolites (e.g., amyloid) from the Central Nervous System. Dwindling CSF dynamics greatly harms the interstitial environment of neurons (occurs mostly with aging) [11].

Alzheimer as discussed previously is more susceptible to elderly people. In brain it does not affect different regions simultaneously. AD progresses in stages and is described in terms of incipient (Braak stages III-IV), mild/moderate (Braak stages IV-V) and severe AD (Braak stages V-VI) [12].While some previous works are focused on genes that have differential topology in gene co expression networks corresponding to different brain regions and to observe the difference in AD severity across regions [13], our objective is to find genes that have differential topology in gene co expression networks corresponding to different stages of AD progress and to find out genes/pathways which are responsible for AD spreading.

III. METHODOLOGY

A. Network Construction

We use the method proposed by Ruan and Zhang [14] for network construction where adjacency measure between a pair of genes is being judged through Pearson’s correlation. In the beginning we are assuming that it is a fully connected network where the nodes are genes and connection-strength is the weight of edges.

We are evaluating the Topological Overlap (T.O.)
between two networks for both weighted and unweighted versions. The corresponding flowchart of the entire process is given in Fig. 1.

\[
\begin{align*}
\text{Network 1: Control and Moderate} & \quad \text{Network 2: Control and Severe} \\
\text{Find the D.E genes} & \quad \text{Find the D.E genes} \\
\text{Take common D.E genes between two networks} & \\
\text{Go for significant interactions corresponding to common D.E genes in two networks} & \quad \text{Go for correlations corresponding to common D.E genes in two networks} \\
\text{Find two correlation matrices corresponding to common D.E genes in two networks} & \\
\text{Go for multiplication operation of the correlation matrices and add all the elements of individual rows} & \\
\text{Evaluation of T.O. via (3)} & \quad \text{Evaluation of T.O. via (4)} \\
\end{align*}
\]

Fig. 1. Flowchart of weighted and unweighted T.O. analysis.

As shown in the flow chart (Fig. 1) we have taken two networks each of them having two sub-networks. Genes in both of the networks are common, but alter in expression levels. In the first network they are control (not affected by A.D) and moderately affected. In the second network they are control and severely affected.

Next we find Differentially Expressed (D.E) genes in the First network (Differentially Expressed between Control and Moderate) and D.E genes in the second network (Differentially Expressed between Control and Severe). Finally we come up with common D.E genes between two networks similar to [13].

### B. Unweighted T.O. Analysis

After finding the common D.E genes between two networks we are taking help of PCIT [15] analysis to find out significant interaction(s) between every pair of genes. In Fig. 1 after taking the common D.E genes the left branch of the tree corresponds to unweighted T.O measure

**PCIT:** Let there be 3 genes x, y, z. Amongst these genes let x and y be connected directly and they are connected via z too. So in between 2 genes there is direct physical gene interaction and via 3rd gene has got indirect physical gene interaction. By this method which gene interaction is direct is done by 2 steps:

1) **Partial correlations:** For every trio of genes in x, y and z, the first three order partial correlation coefficients are computed by:

\[
R_{xy,z} = \frac{R_{xy} - R_{xz} R_{yz}}{\sqrt{(1 - R_{xz}^2)(1 - R_{yz}^2)}}
\]

and similarly for \( R_{xz,y} \) and \( R_{yz,x} \)

The partial correlation between x and y given z (here denoted by \( r_{xy,z} \)) indicates the strength of the linear relationship between x and y that is independent (uncorrelated with) of z.

2) **Information theory:** This is invoked from the concept of DPI (Data Processing Inequality) [16].

We get the tolerance level/threshold for each association

\[
\varepsilon = \left( \frac{R_{xy,z}^2 + R_{xz,y}^2 + R_{yz,x}^2}{3} \right)
\]

After applying the PCIT algorithm we get corresponding to every gene which other genes (columns) have got significant interactions.

Let \( a \) be a matrix whose entries signify interactions. After the application of PCIT if the interaction between \( i \) th row and \( j \) th column is significant then the corresponding entry \( a_{ij} = 1 \) else \( a_{ij} = 0 \). In this way two matrices are formed for the two networks. Next we explore which interactions are significant and common between two networks for each gene. Let for gene \( i \) in network 1 \( X \) no of interaction(s) is/are significant, and in network 2 it is \( Y \). So as in [13] the T.O. of gene \( i \) between two networks can be defined as

\[
T.O. = \frac{X \cap Y}{\max(X,Y)}
\]

**C. Weighted T.O. Analysis**

Unlike unweighted concept here we retain with the correlation values between each pair of common D.E genes for the two networks. This is followed by our multiplication operation of the two correlated matrices. Finally we add up the gene-gene interactions per gene to determine the corresponding gene’s proportional T.O significance. In Fig. 1 after taking the common D.E genes the right branch of the tree corresponds to weighted T.O measure.

Here, we found the significance of gene \( i \) in both networks after conducting the multiplication and addition operations of the two correlated matrices. Hence, the \( i \) th entry possessing a high value highlights that the correlative significance of \( i \) th gene with other genes in both networks is very strong whereas if the \( i \) th entry has got a low value, it clarifies that the correlative significance of \( i \) th gene with the other genes is quite weak.

After multiplication (of two matrices) and addition of the two correlated matrices. Hence, the \( i \) th entry possessing a high value highlights that the correlative significance of \( i \) th gene with other genes in both networks is very strong whereas if the \( i \) th entry has got a low value, it clarifies that the correlative significance of \( i \) th gene with the other genes is quite weak.

After multiplication (of two matrices) and addition of the two correlated matrices. Hence, the \( i \) th entry possessing a high value highlights that the correlative significance of \( i \) th gene with other genes in both networks is very strong whereas if the \( i \) th entry has got a low value, it clarifies that the correlative significance of \( i \) th gene with the other genes is quite weak.

After multiplication (of two matrices) and addition of the two correlated matrices. Hence, the \( i \) th entry possessing a high value highlights that the correlative significance of \( i \) th gene with other genes in both networks is very strong whereas if the \( i \) th entry has got a low value, it clarifies that the correlative significance of \( i \) th gene with the other genes is quite weak.
After getting the T.O value for each common D.E. gene we go for the permutation test [17]. Depending upon the result of the permutation test we proceed for ranking.

D. Pre-Processing

We have taken the dataset from publicly available database [18]. As the size of the dataset is very high (54,675 genes with 30 time instants), so the time as well as space complexity is very high if we are about to analyze the entire dataset. For this reason before going for detailed analysis we have to go for some pre-processing. There are two stages, they are

1) The skewness of the dataset is high, for different entries. To remove the skewness we go for ‘log-normal’ distribution. This makes the distribution of the dataset somehow uniformly distributed.
2) In the second stage we evaluate the standard-deviation of all genes over different expression levels. Setting a threshold value we fetch the expression values of the corresponding genes which give a standard-deviation greater than the threshold.

IV. RESULTS AND DISCUSSION

As mentioned in the previous section the original dataset has 54,675 entries. After applying the pre-processing strategies the total entries get reduced to 10,000 (We are choosing top 10,000 genes). We have restricted our work between control and moderate and control and severe. We are not taking incipient stage into our account because the change of expression levels between control and incipient is not so prominent.

First, we had to find the D.E genes between control and moderate and control and severe. We have done this by DEGseq (R) [19] (It is a package to find the Differentially Expressed genes from the gene expression value itself. Here depending upon expression values of genes at different time instants and by a particular threshold ‘p-value’/’z-score’/’q-value‘ D.E genes are computed). This validation/significance of our method has been done through the following steps:

1) We have searched the significance of the T.O values for all the 66 common D.E. genes (for both weighted and unweighted measure) by random permutation test/‘t’-test.
2) Based upon the result of the permutation test/‘t’-test the 66 common D.E. genes are ranked
3) We have also computed the ranking of 66 common D.E. genes by Diffrank [20].
4) Next we have fetched top 15 ranked genes(approximately top 25% of common D.E. genes) (from both weighted and unweighted measure) computed by proposed one as well as by Diffrank.

After fetching the top 15 genes we have found that the number of common genes between proposed method and Diffrank are very low. Out of top 15 genes in weighted measure only 4 genes are common and in unweighted measure only 3 genes are common.

5) Next we have found GO term based significance as well as pathways based significance of the top 15 ranked genes by [21], [22].

In Tables I, II, III, and IV we have enlisted significant G.O. terms and KEGG pathways along with ‘p-value’ and number of O.R.F name of the genes associated with them. Here we have found that out of the 15 top D.E genes most of them have associated differently to form different G.O. terms as well as pathways.

<table>
<thead>
<tr>
<th>GO-Terms</th>
<th>‘p-value’</th>
<th>Genes</th>
<th>GO-Terms</th>
<th>‘p-value’</th>
<th>Genes</th>
</tr>
</thead>
<tbody>
<tr>
<td>GO:0046885</td>
<td>0.0346</td>
<td>2</td>
<td>tref1, kynu</td>
<td>GO:0006569</td>
<td>0.0348</td>
</tr>
<tr>
<td>GO:0032350</td>
<td>0.0346</td>
<td>3</td>
<td>kynu, usp28, itgb3</td>
<td>GO:0046218</td>
<td>0.0348</td>
</tr>
<tr>
<td>GO:0006569</td>
<td>0.0349</td>
<td>2</td>
<td>jak1, efca2</td>
<td>GO:0002070</td>
<td>0.0352</td>
</tr>
<tr>
<td>GO:0046218</td>
<td>0.0349</td>
<td>2</td>
<td>cog3, efca2</td>
<td>GO:0005131</td>
<td>0.0359</td>
</tr>
<tr>
<td>GO:0004718</td>
<td>0.0352</td>
<td>1</td>
<td>fancd2</td>
<td>GO:0002064</td>
<td>0.0359</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>GO-Terms</th>
<th>‘p-value’</th>
<th>Genes</th>
<th>GO-Terms</th>
<th>‘p-value’</th>
<th>Genes</th>
</tr>
</thead>
<tbody>
<tr>
<td>GO:0015459</td>
<td>0.00095</td>
<td>2</td>
<td>kcne1, mmp10</td>
<td>GO:0030303</td>
<td>0.019</td>
</tr>
<tr>
<td>GO:0016247</td>
<td>0.00162</td>
<td>2</td>
<td>tp73, kcnmb2</td>
<td>GO:0018676</td>
<td>0.019</td>
</tr>
<tr>
<td>GO:0015457</td>
<td>0.00162</td>
<td>3</td>
<td>ciao1, kcne1, mmp10</td>
<td>GO:0036767</td>
<td>0.019</td>
</tr>
<tr>
<td>GO:0030303</td>
<td>0.0093</td>
<td>3</td>
<td>trim14, tp73, cdc20b</td>
<td>GO:0019113</td>
<td>0.027</td>
</tr>
<tr>
<td>GO:0008076</td>
<td>0.0093</td>
<td>2</td>
<td>mmp10, kcnmb2</td>
<td>GO:0018675</td>
<td>0.0274</td>
</tr>
</tbody>
</table>
Table III: Significant pathways in proposed method as well as in DIFFRANK by weighted measure

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Tryptophan metabolism</td>
<td>0.0220</td>
<td>3 kynu, cog3, efca2</td>
<td>Jak-STAT signalling pathway</td>
<td>0.0212</td>
<td>3 jak1, kcn1, trv3</td>
</tr>
<tr>
<td>Pancreatic cancer</td>
<td>0.0383</td>
<td>3 jak1, itgb3, usp28</td>
<td>Tryptophan metabolism</td>
<td>0.0220</td>
<td>3 csh1, kynu, mmp10</td>
</tr>
<tr>
<td>Leishmaniasis</td>
<td>0.0399</td>
<td>2 usp28, efca2</td>
<td>Pancreatic cancer</td>
<td>0.0383</td>
<td>2 cia01, cog3</td>
</tr>
<tr>
<td>Arrhythmogenic right ventricular cardiomyopathy</td>
<td>0.0416</td>
<td>2 efca2, cog3</td>
<td>Leishmaniasis</td>
<td>0.0399</td>
<td>1 efca2</td>
</tr>
<tr>
<td>ECM-receptor interaction</td>
<td>0.0459</td>
<td>2 tref1, mge3771</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Hypertrophic cardiomyopathy (HCM)</td>
<td>0.0464</td>
<td>1 c20orf78</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Hematopoietic cell lineage</td>
<td>0.0488</td>
<td>1 fancd2</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table IV: Significant pathways in proposed method as well as in DIFFRANK by unweighted measure

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>p53 signaling pathway</td>
<td>0.0253</td>
<td>3 tp73, cdc20b, mmp10</td>
<td>Linoleic acid metabolism</td>
<td>0.0212</td>
<td>2 cyp2c9, plxnd1</td>
</tr>
<tr>
<td>Vascular smooth muscle contraction</td>
<td>0.0424</td>
<td>2 kcnmb2, efca2</td>
<td>Arachidonic acid Metabolism</td>
<td>0.0422</td>
<td>2 itgb3, cia01</td>
</tr>
<tr>
<td>Neurotrophin signaling pathway</td>
<td>0.0460</td>
<td>2 kcnmb2, trim14</td>
<td>Retinol metabolism</td>
<td>0.0472</td>
<td>1 kcnmb2</td>
</tr>
</tbody>
</table>

Top 25% ranked genes have been selected based upon their low T.O score because our main concern is to select condition specific genes. Thus top 25% genes sharing less number of neighbors than others (in different conditions) are selected. They have more enriched G.O. terms as well as more enriched biological pathways than the remaining low ranked genes, so to check the effectiveness of the proposed method we have opted to compare top 25% genes from both methods.

From Tables I, II, III, and IV (List is prepared according to their ‘p’-value as well as the impact of these G.O. terms/paths in A.D. described in different literature) it is evident that our proposed methodology gives better result than DIFFRANK both in terms of G.O enrichment analysis as well as of pathway analysis.

Our method shows better result because the existing method [20] focuses on local (differential connectivity which is the local difference between two networks calculated by the number of genes associated with a particular gene) as well as on global concept (between centrality: which calculate the change in the expression levels of central genes), but as given in [13] A.D does not affect all the brain regions at a time but there are differences in AD severity across regions. So it shows more local phenomena than the global one. In general all the genetic diseases show this kind of pattern. It [20] also shows a problem of controlling the value of the trade-off parameter (λ), trying to make up a balance between local and global connectivity. So the optimality of the result is solely dependent on this parameter, making the problem more parameter driven. Here we proposed an extended version of an existing method [13] and we have shown that it outperforms other existing method [20].

In Tables I, and II we have enlisted some significant G.O. terms. Some of the G.O terms found by the proposed method are responsible for generation and spreading of A.D in Human and other primates. They have been verified in some recent literatures like: GO:0046885(regulation of hormone biosynthetic process)[23], GO:0032350(regulation of hormone metabolic process)[24], GO:0006569(tryptophan catabolic process)[25], GO:0046218(indolalkylamine catabolic process)[26], GO:0004718(protein tyrosine kinase activity)[27], GO:0015459(potassium channel regulator activity)[28], GO:0016247(channel regulator activity)[29], GO:0015457(Transport)[30], GO:0008076(voltage-gated potassium channel complex)[31].

Again in Tables III and IV we have listed some significant pathways. Some of them also verified to be responsible for generation and spreading of A.D in some recent literatures like: Tryptophan metabolism and Leishmaniasis [32], Arrhythmogenic right Ventricular cardiomyopathy [33], ECM-receptor interaction [34], Hypertrophic cardiomyopathy [35], Hematopoietic cell lineage [36], p53 signaling pathway [37], Neurotrophin signalling pathway [38], Retinol metabolism [39].

V. CONCLUSION AND FUTURE WORK

In this work we have done T.O. analysis from D.E. genes. D.E. genes are found by comparing the gene-expression values between two states/regions. As discussed in the result and discussion section first we have searched for common D.E genes between two networks, this common set of
genes (D.E) will act differently in the two networks (first network comprises control and moderately affected genes and the second network comprises control and severely affected genes).

Next to find the unweighted T.O. measure we have searched for significant gene to gene interactions (by the common D.E genes) in both networks and then the common interactions between them.

In weighted T.O measure instead of significant gene to gene interactions we have to focus on each and every interaction. So here we have searched for correlation matrices of the common D.E genes in both networks, then we have gone for multiplication and addition operations over the correlation matrices.

Basically here we have developed a new approach to find the T.O value. Other existing method [13] focuses only on unweighted T.O measure which takes into account only of some significant gene to gene interactions. So the overall gene dependency and gene significance in a particular network is not totally highlighted. On the other side weighted T.O measure focuses on each and every interaction how strong or weak it is, and accordingly we can get a clear picture of gene dependency and gene significance in a network. In Tables III, and IV we can observe this where the number of enriched biological pathways in weighted measure is more than the unweighted counterpart.

Here we have also proposed a novel concept of ranking based upon the T.O. measure, which unlike [20] does not depend upon any local or global measure or any trade-off parameter, thus gives a better result than the existing method of ranking [20].

Maintaining this line of thought our next step being finding out D.E genes from gene expression values and phenotype specific traits. In such a context, we are interested to explore this idea through linear and non-linear methodologies. Accordingly, in the linear method we will find the correlation between gene expression values and phenotype specific trait whereas in the non-linear method we will go through mutual information and/or polynomial and spline regression model based measure of dependency between them. This would probably allow us to check the compatibility of trait specific analysis by comparing the result with other existing methods.

REFERENCES


---

**Aurpan Majumder** had obtained his B.Tech. in 2002 in electronics & telecommunication Engg. from Haldia Institute of Technology, India and M.Tech. in 2005 in computer science from Jadavpur University, India. Currently, he is working as an assistant professor at National Institute of Technology, Durgapur, India. He is pursuing PhD in the domain of gene differential coexpression analysis. His research interests also include biomedical signal and image processing.

**Mrityunjay Sarkar** had obtained his B.Tech. in electronics and communication, Eng. from Asansol Eng. College and M.Tech. in telecommunication engineering from National Institute of Technology Durgapur. He is now working as an asst. prof. in Durgapur Institute of Advanced Technology and Management, Durgapur in the department of Electronics and Communication Eng. His research areas of interest being Image Processing, Soft Computing, Gene Co-Expression Network Analysis.